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UNIVERSITY OF  
**Southampton**  
Faculty of Engineering & the Environment

# Secondary noise sources in a vortical flow interacting with an undulated aerofoil

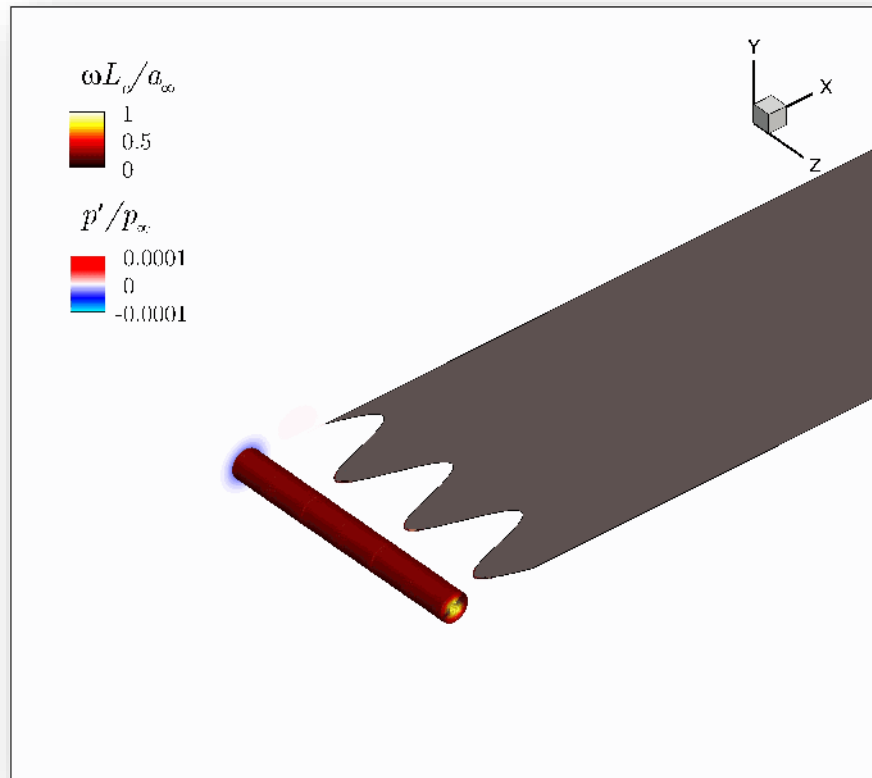
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# Background & Introduction

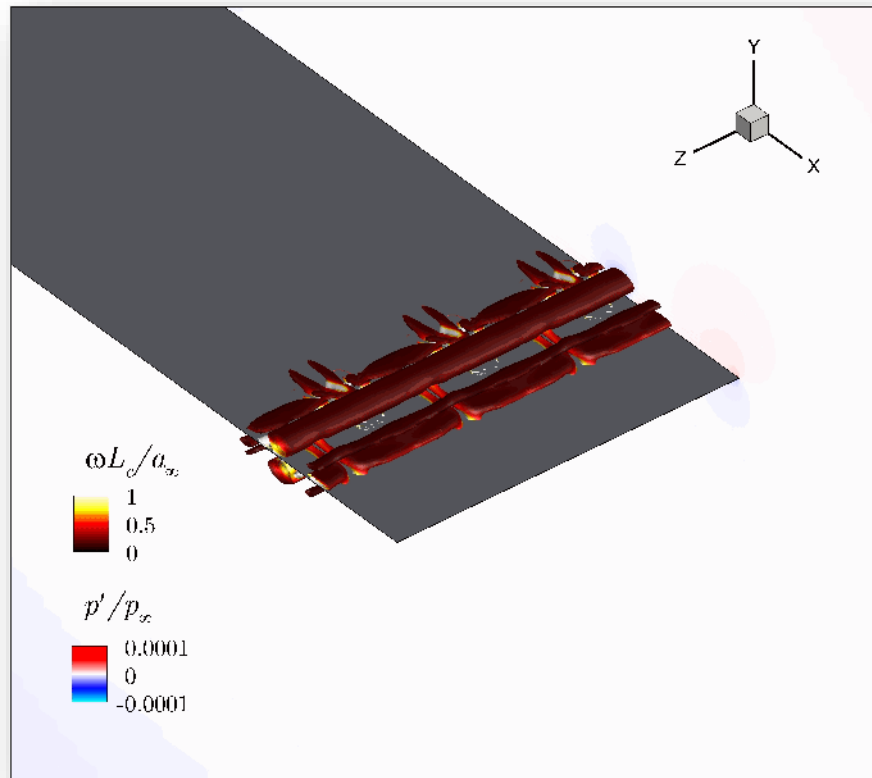
# Primary Source (S1)

- LE vortical scattering (LEVS)
  - LEVS sound can be obtained by using an semi-infinite aerofoil.



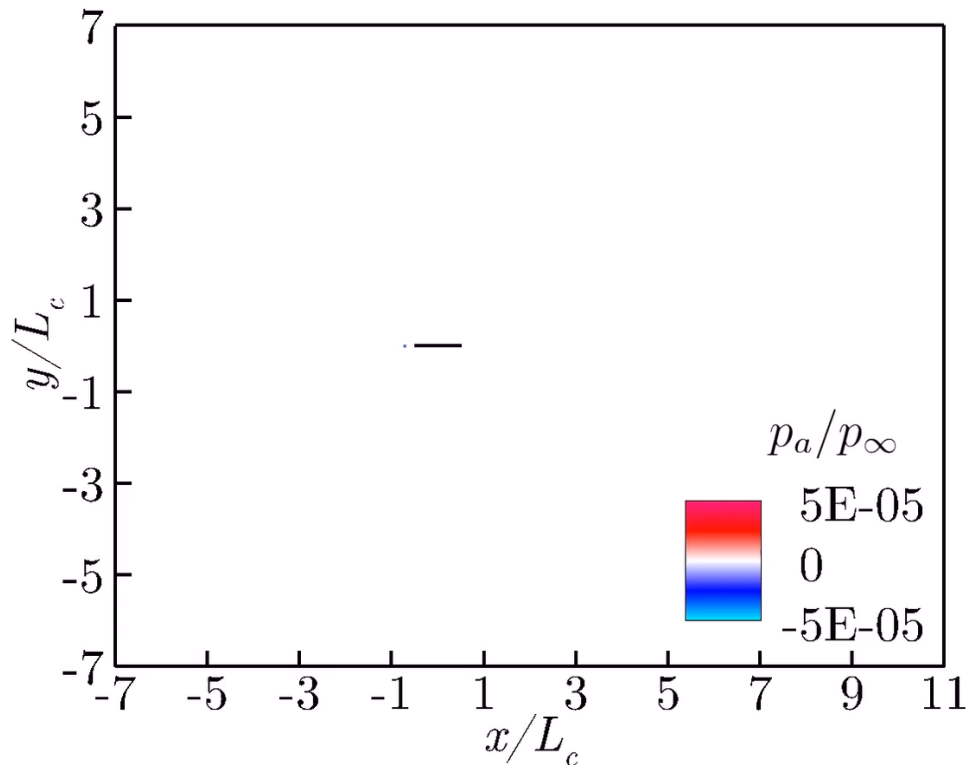
# Secondary Source (S2-TEVS)

- Trailing-edge vortical scattering (TEVS)
  - The vortex has been bisected and distorted at LE before reaching TE.



# Secondary Source (S2-ABS)

- Acoustic back-scattering (ABS)
  - Subsequent scattering and reflection of sound waves having been generated by the vortex at LE or TE.



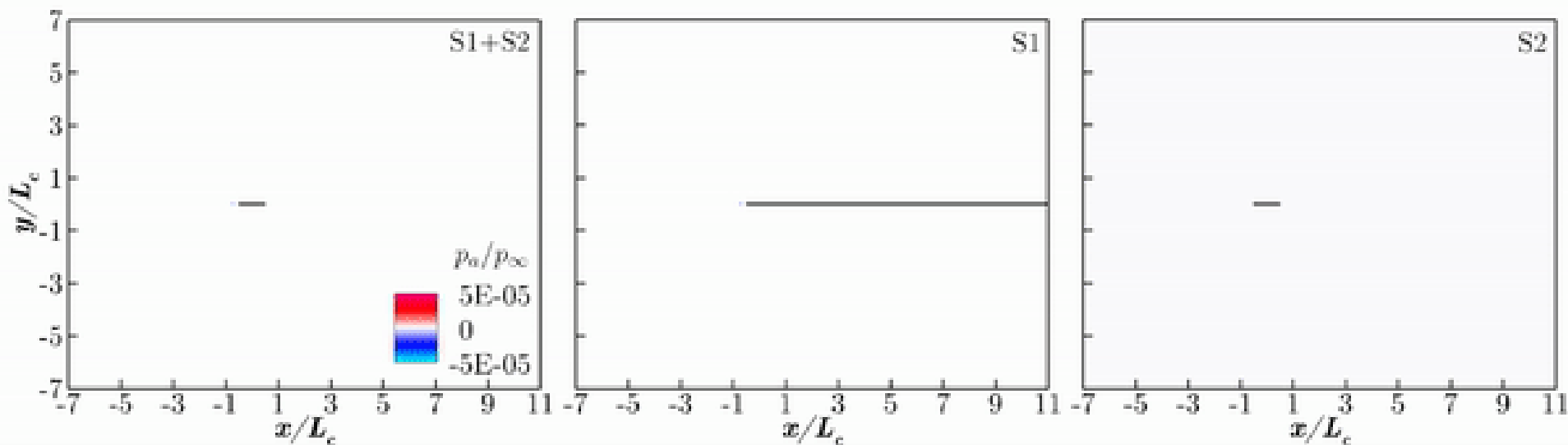
# Why on Secondary Sources?

- Not much known, particularly, about the contribution of TEVS (and its ABS).
  - Even for SLE cases, let alone the WLE.
  - Amiet's theory (1975) covers LEVS and its ABS only.
- New results exhibit significant effects at high frequencies where the WLE geometry works.
- What implications do the secondary sources have in terms of the noise reduction by using WLE?

# Results

# The Presence of TE

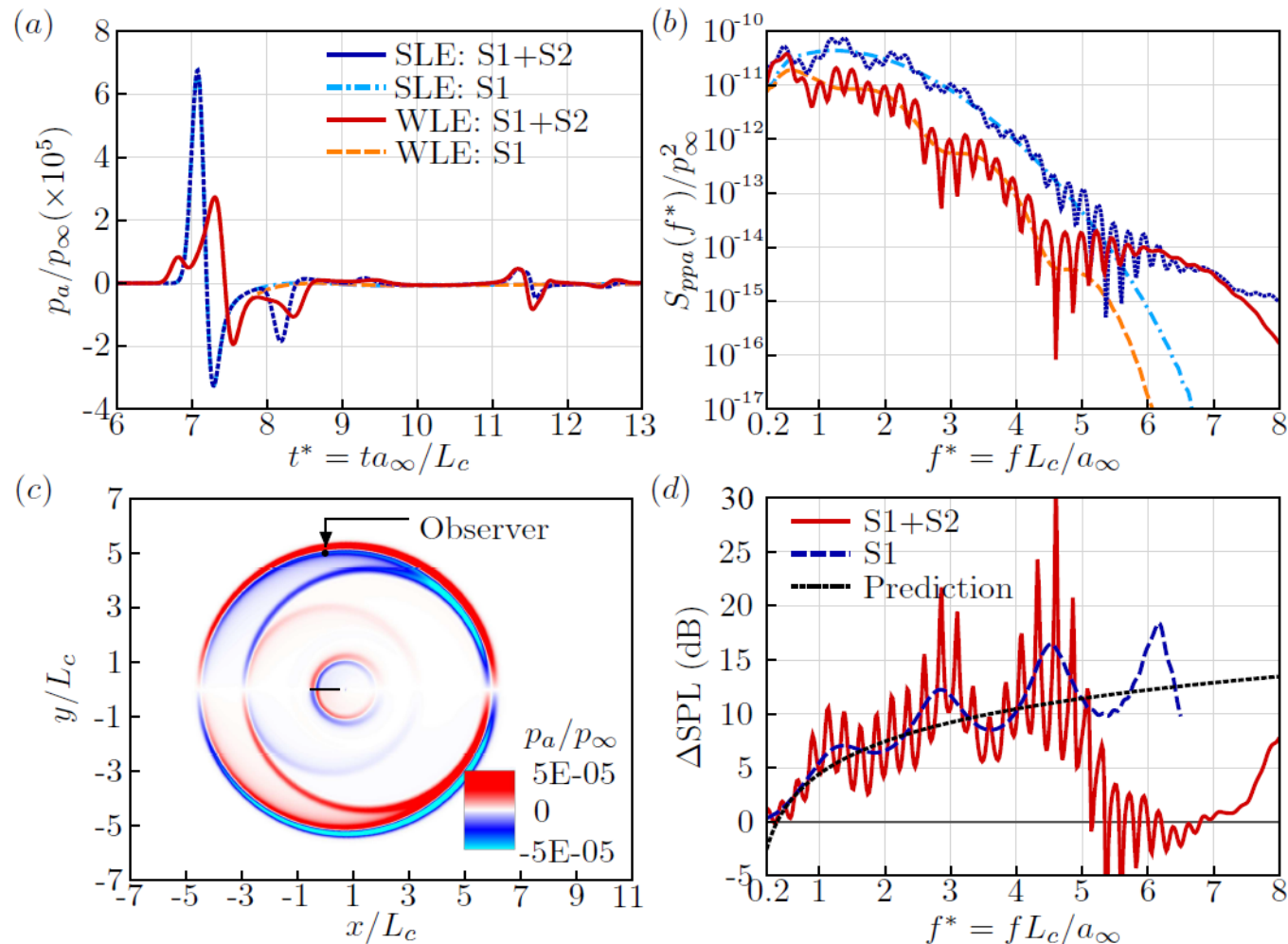
- $S1+S2$  = All sources combined (i.e. finite chord)
- $S1$  = Primary source = LEVS (i.e. semi-infinite chord)
- $S2$  = Secondary sources = TEVS + ABS





# S2 Effects on Sound PSDs

- Significant changes in the high-frequency range

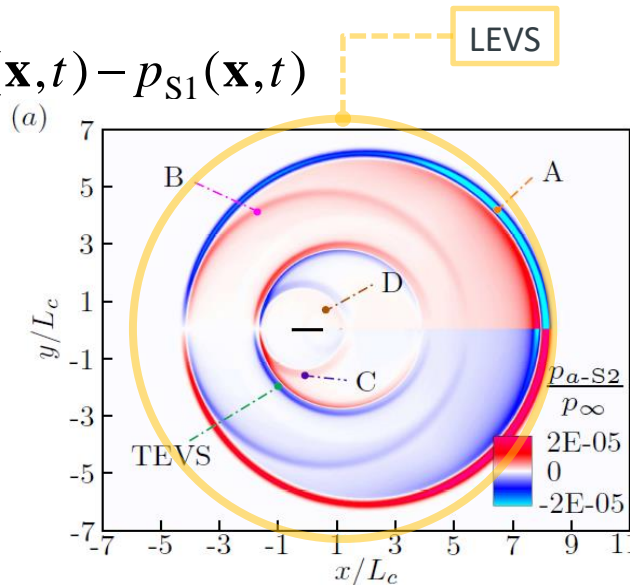


# Extracting S2 Solution

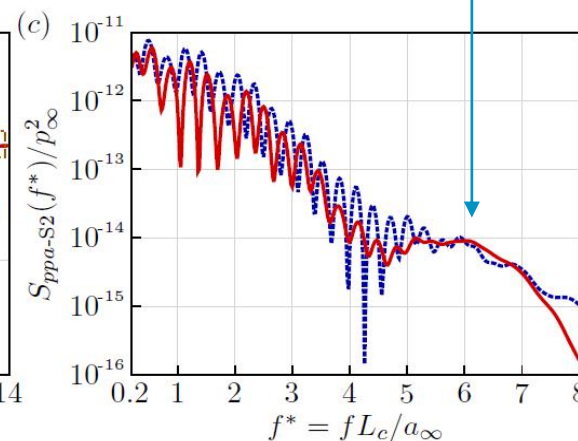
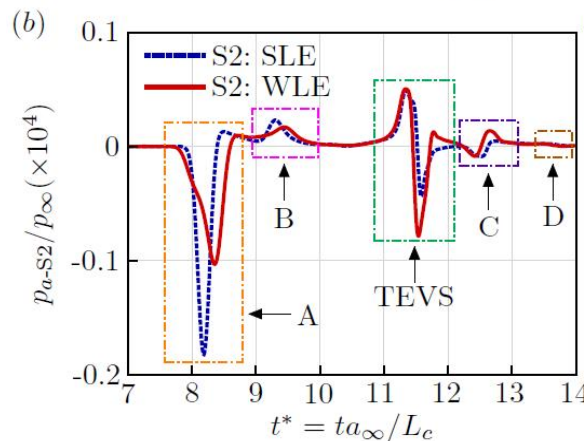
- Subtracting the SIC solution from the FC solution:

$$p_{S2}(\mathbf{x}, t) = p(\mathbf{x}, t) - p_{S1}(\mathbf{x}, t)$$

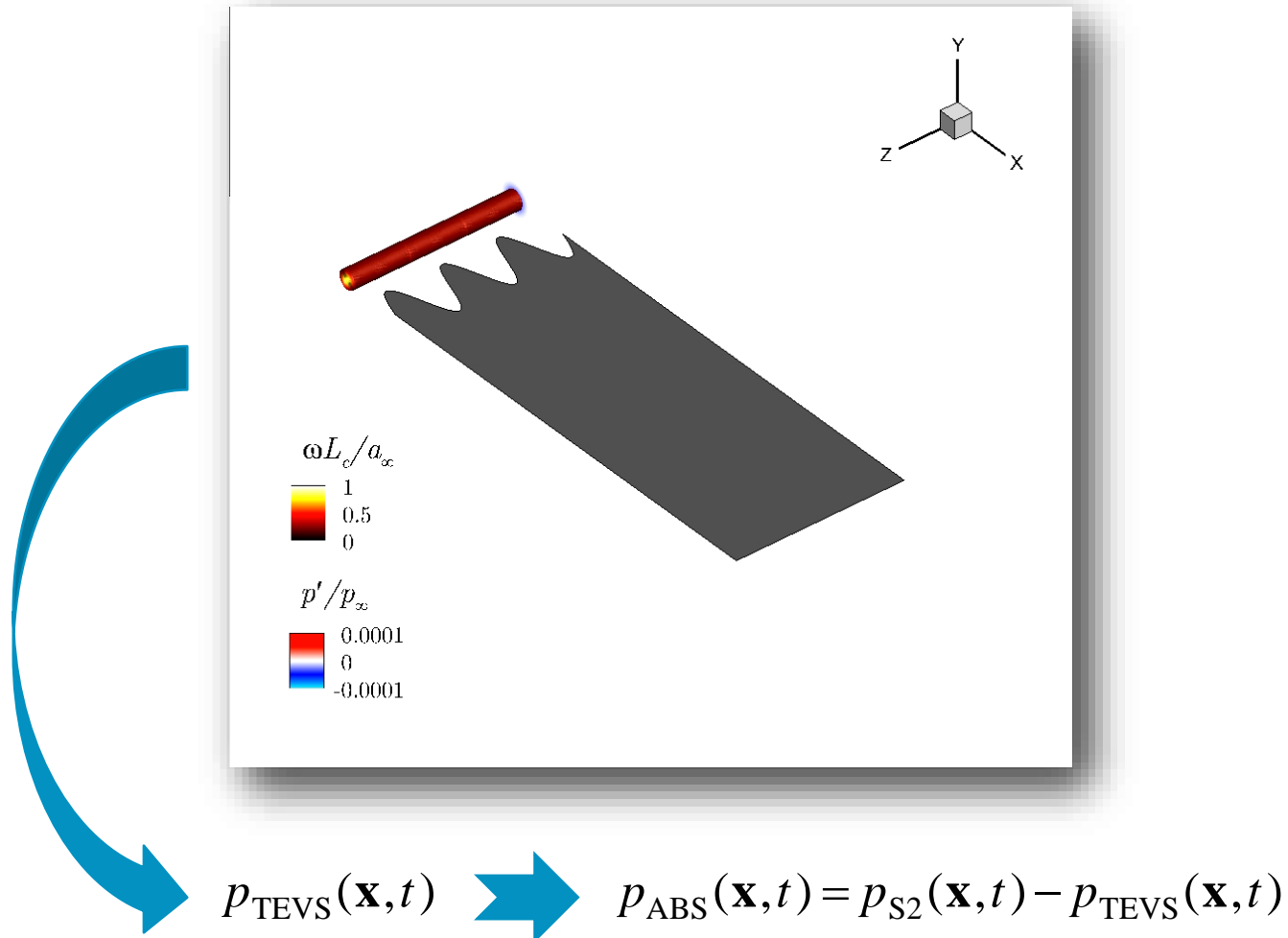
$$\begin{cases} p(\mathbf{x}, t) : \\ p_{S1}(\mathbf{x}, t) \end{cases}$$



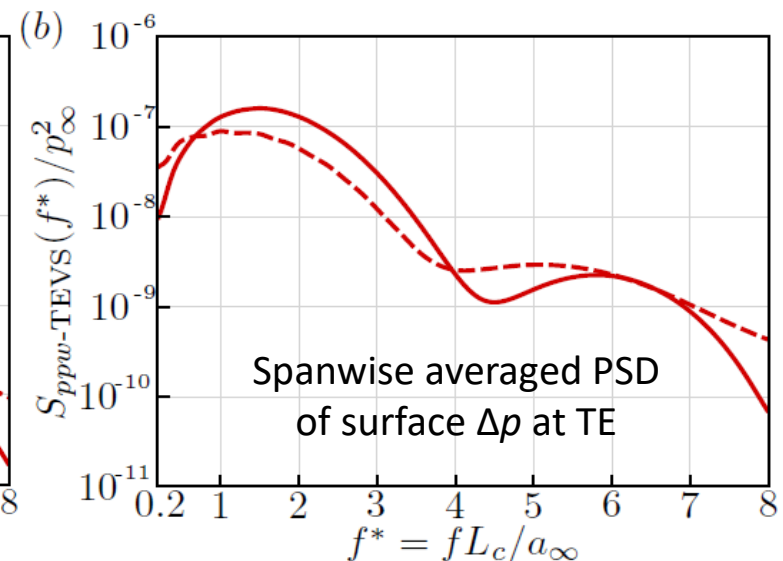
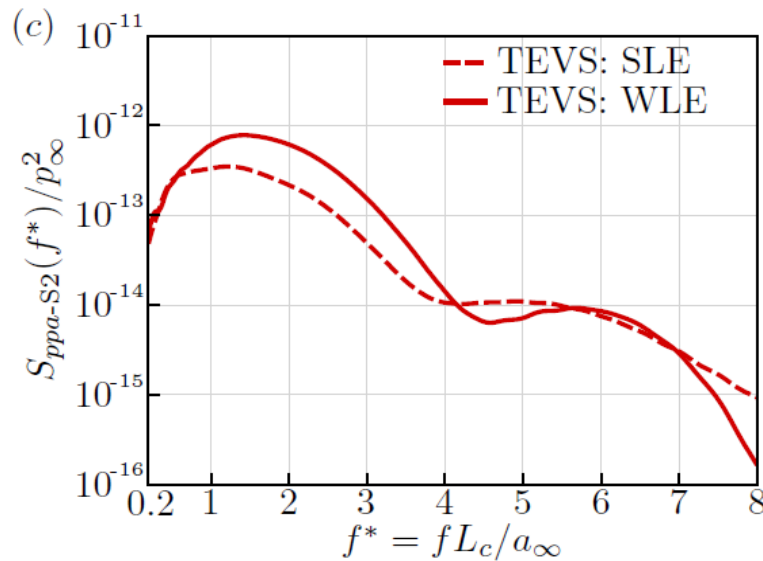
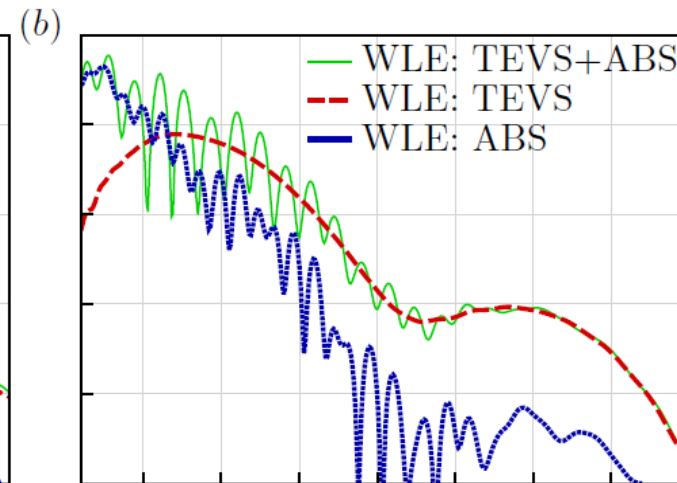
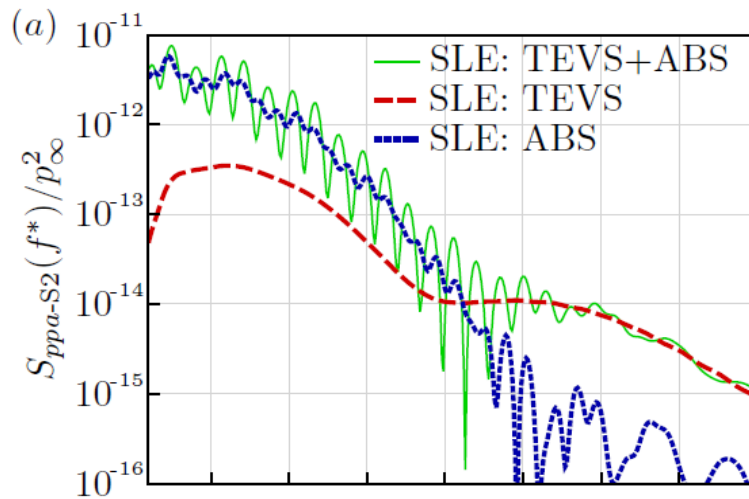
Which one is responsible,  
TEVS or ABS?



# Extracting TEVS Solution



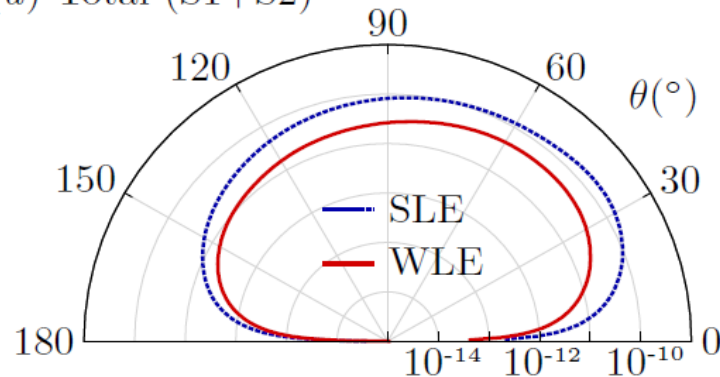
# TEVS vs ABS



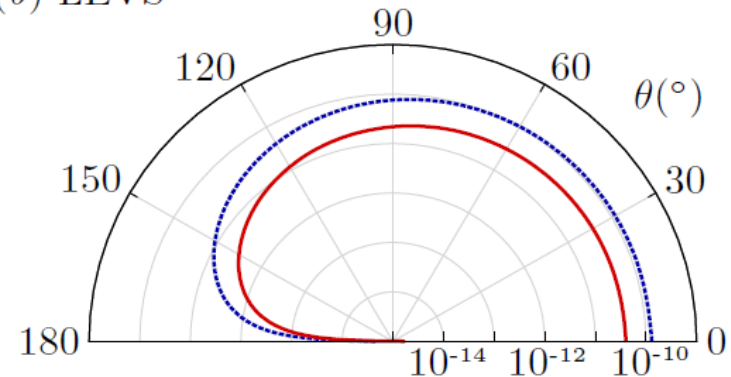
# Overall SPL Directivity

- For each source compared to all combined (log scale):

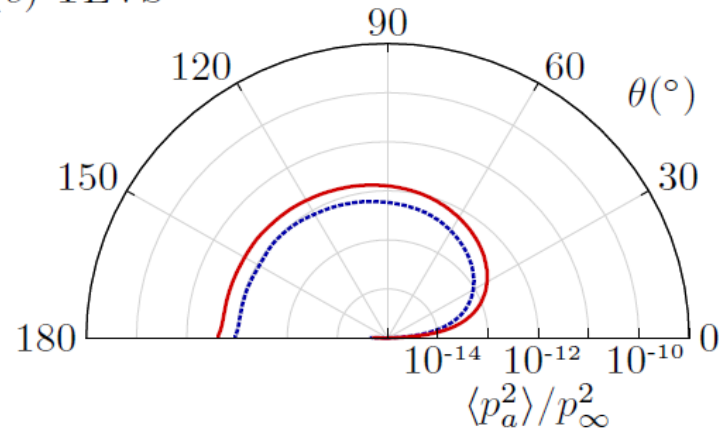
(a) Total (S1+S2)



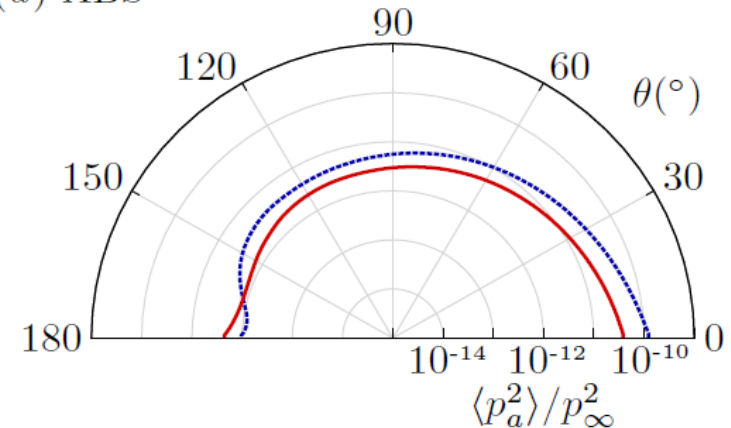
(b) LEVS



(c) TEVS

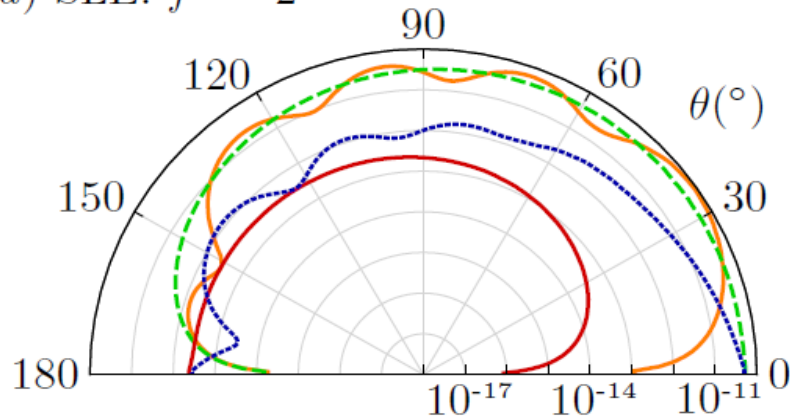


(d) ABS

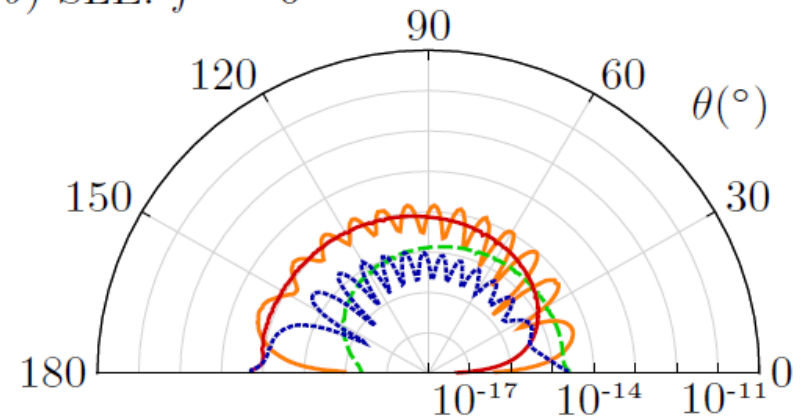


# Low vs. High Frequencies

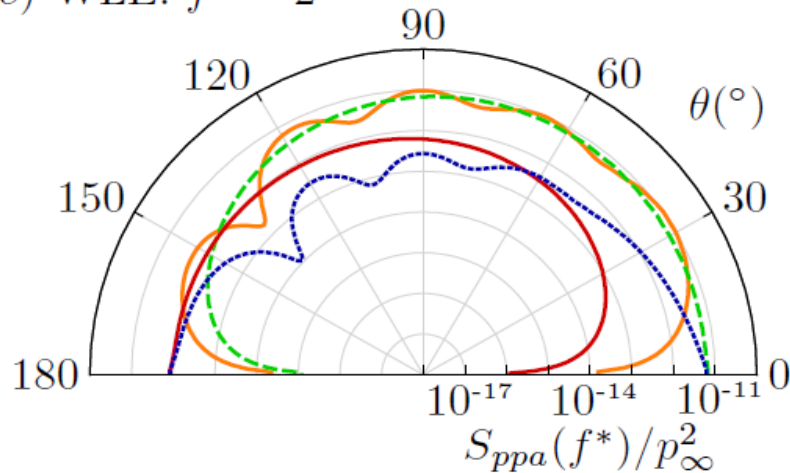
(a) SLE:  $f^* = 2$



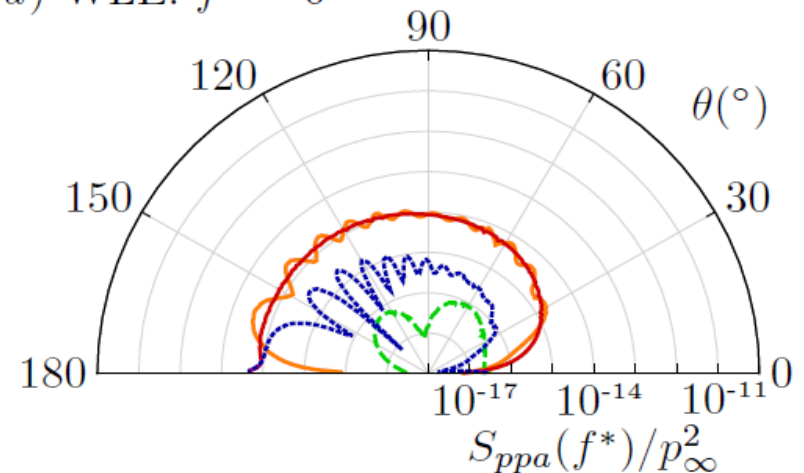
(b) SLE:  $f^* = 6$



(c) WLE:  $f^* = 2$



(d) WLE:  $f^* = 6$



— Total

- - - LEVS

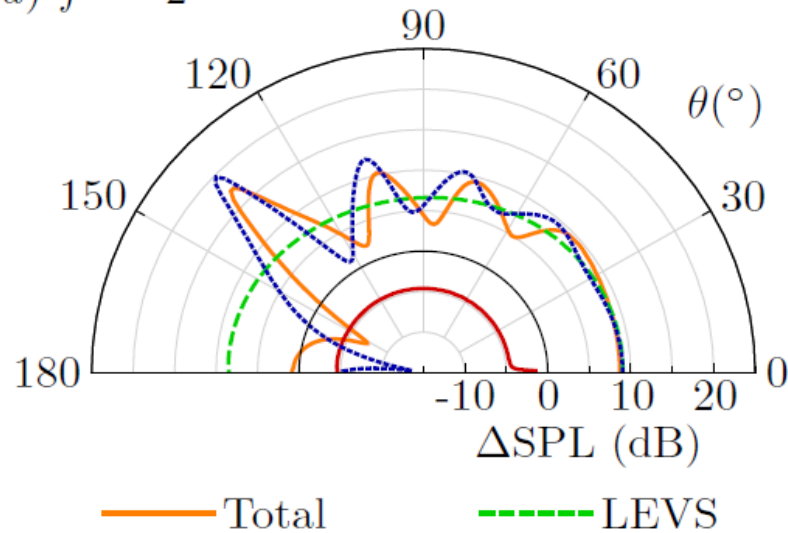
— TEVS

— ABS

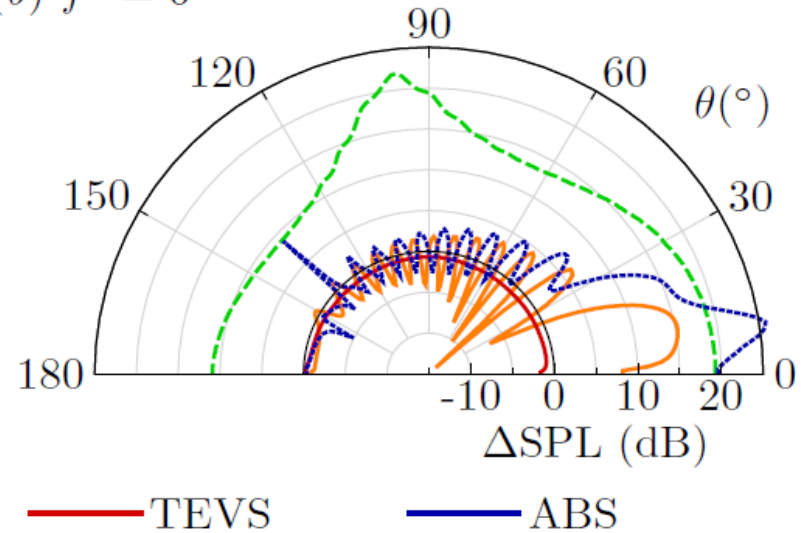
# Noise Reduction by WLE (?)

- Prediction of noise reduction based on the primary source (LEVS) becomes unreliable.

(a)  $f^* = 2$



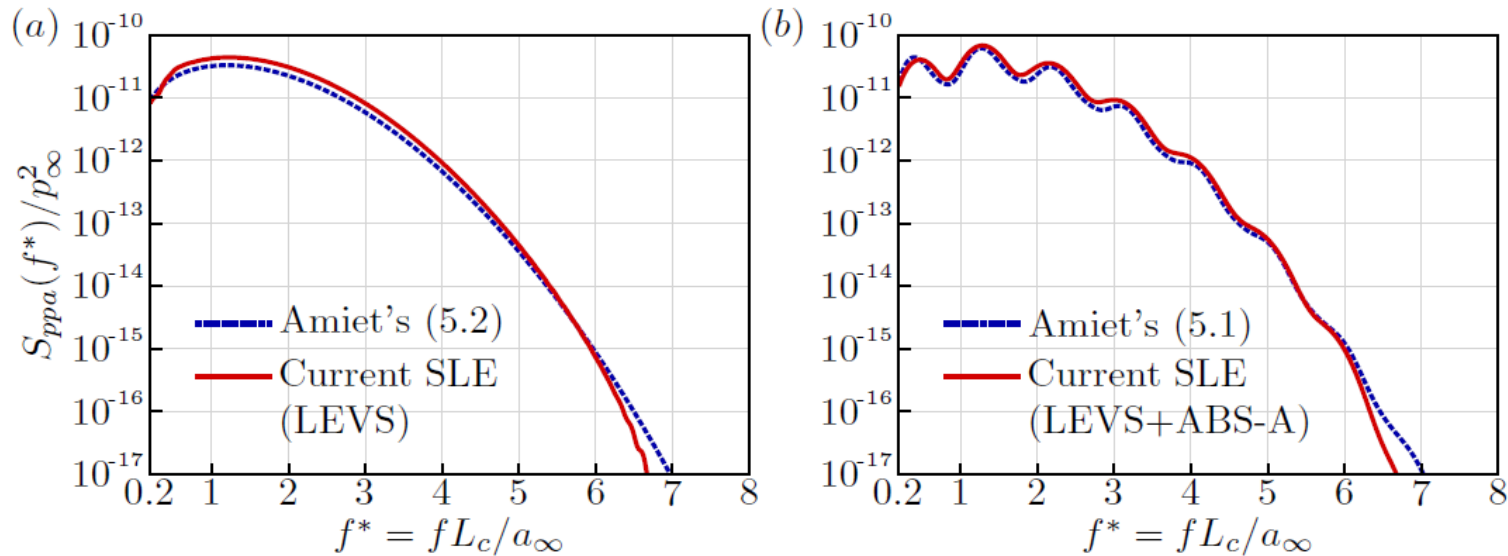
(b)  $f^* = 6$





# Analytic Prediction (2D/SLE)

- Amiet's model for ATI noise (JSV 1975)



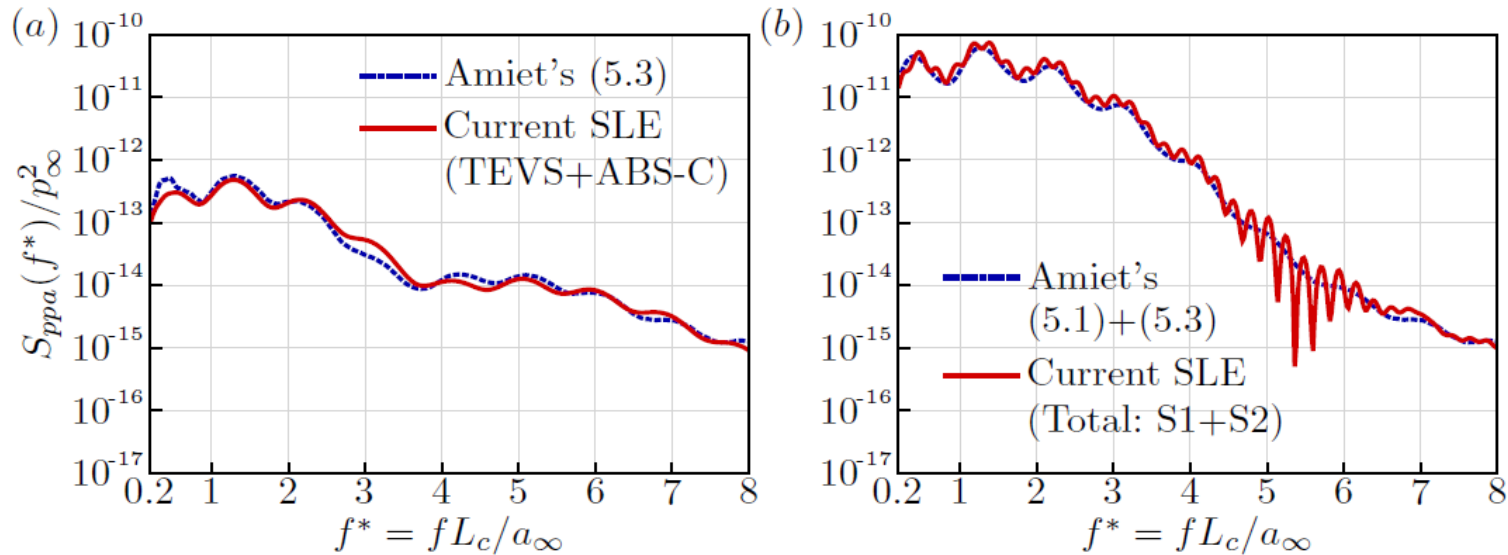
$$S_{ppa\text{-Amiet1}}(k_x) = \frac{\pi k_x M_\infty \rho_\infty^2 u_\infty^2 L_c^2 \sin^2 \theta}{8r_o A^3(\theta)} \Phi_{vv}(k_x) |\mathcal{L}(k_x)|^2$$

$$S_{ppa\text{-Amiet1-LEVS}}(k_x) = \frac{\rho_\infty^2 u_\infty^2 (1 - M_\infty) \sin^2 \theta}{2\pi r_o k_x A(\theta)^2 [A(\theta) - \cos \theta]} \Phi_{vv}(k_x)$$



# Analytic Prediction (2D/SLE)

- Amiet's model for self-noise due to TBL at TE (JSV 1976):



$$S_{ppa-Amiet2}(k_x) = -\frac{\beta^2 \mu_0^2}{16} (y_{TE} - y_o)^2 \iint \frac{S_{QQ}(x_1, x_2, k_x)}{R(x_1)R(x_2)} \times \\ H_1^{(2)}(S(x_1))H_1^{(1)}(S(x_2))dx_1dx_2$$

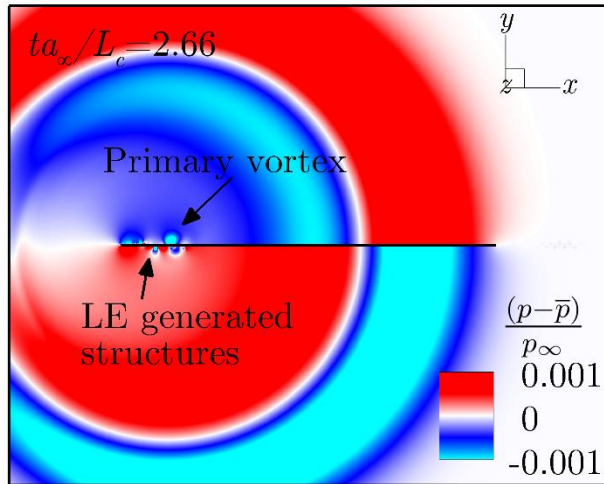
$$R(x) = \sqrt{(x - x_o)^2 + \beta^2(y_{TE} - y_o)^2}, \quad S(x) = \mu_0[M_\infty(x - x_o) + R(x)]$$

# Concluding Remarks

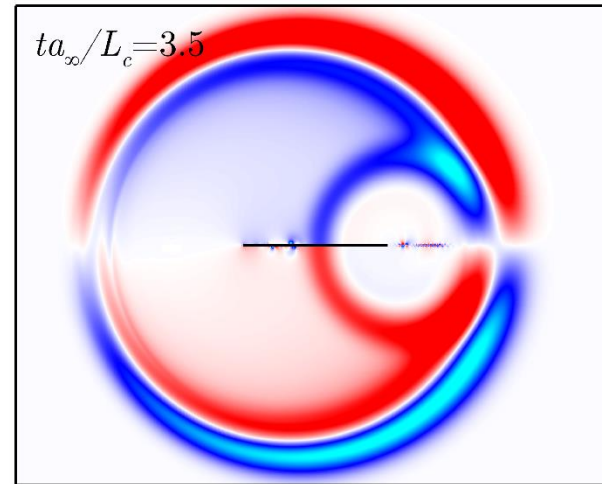
- The dominance of TEVS at high frequencies:
  - effectively acts as the primary source in all directions.
  - limits the noise-reduction performance of WLE.
  - adverse effect at low frequencies (TEVS amplified by WLE).
- Perhaps false accusation on broadband self-noise?
- Narrow angle of sound measurement ( $50^\circ \leq \theta \leq 130^\circ$ ) sound?
- Provisions for analytic prediction models for ATI noise:
  - to include the effect of TEVS.

# Two-dimensional simulation

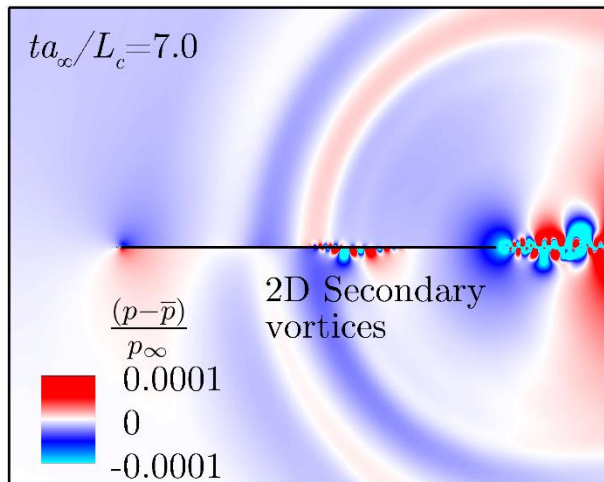
Leading-edge vortical scattering



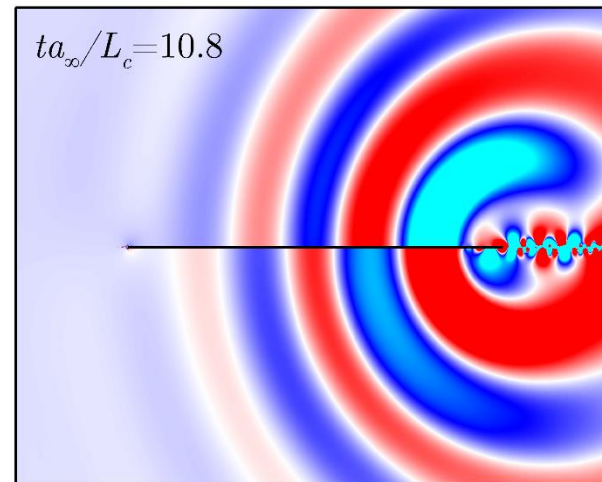
Acoustic backscattering



Trailing-edge vortical scattering  
(primary vortex)



Trailing-edge vortical scattering  
(secondary vortices)



# Three-dimensional simulation

- Three dimensional strong vortex interaction,  $|u'| = 0.25U_\infty$

$$ta_\infty/L_c = 1.534$$

